

Small Angle Shubnikov-de Haas Measurements in Silicon MOSFET's: the Effect of Strong In-Plane Magnetic Field.

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Measurements in magnetic fields applied at small angles relative to the electron plane in silicon MOSFETs indicate a factor of two increase of the frequency of Shubnikov-de Haas oscillations at $H > H_{sat}$. This signals the onset of full spin polarization above H_{sat} , the parallel field above which the resistivity saturates to a constant value. For $H < H_{sat}$, the phase of the second harmonic of the oscillations relative to the first is consistent with scattering events that depend on the overlap instead of the sum of the spin-up and spin-down densities of states.

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A great deal of interest has recently been focussed on the anomalous behavior of two-dimensional (2D) systems of electrons [1,2] and holes [3,4,5] whose resistivities unexpectedly decrease with decreasing temperature, behavior that is generally associated with metals rather than insulators [6]. One of the most intriguing characteristics of these systems is their enormous response to magnetic fields applied in the plane of the electrons [7,8,9] or holes [5,10]: the resistivity increases sharply by more than an order of magnitude, saturating to a constant plateau value above a magnetic field H_{sat} .

In this paper we report studies of the resistivity of the 2D electron system in silicon MOSFETs in magnetic fields applied at small angles ϕ with respect to the plane. This allows a study of the Shubnikov-de Haas (SdH) oscillations in perpendicular fields sufficiently small that the orbital motion has a negligible effect on the response to the in-plane component of the magnetic field. At small tilt angles ϕ , the SdH oscillations plotted versus filling factor have twice the period below H_{sat} compared with the period above H_{sat} . This implies that the electron system is fully spin-polarized in high fields, $H > H_{sat}$, where the resistivity has reached saturation. Detailed examination of the oscillations in fields below H_{sat} indicates unusual behavior consistent with electron scattering that depends on the product rather than the sum of the spin-up and spin-down densities of states.

Two silicon MOSFETs with mobilities $\mu \approx 20,000$ V/cm² s at $T = 4.2$ K were used in these studies. Contact resistances were minimized by using samples with a split-gate geometry, which permit high densities in the vicinity of the contacts while allowing independent control of the density of the 2D system under investigation. Standard AC four-probe techniques were used at 3 Hz to measure the resistance in the linear regime using currents typically below 5 nA. Data were taken on samples mounted on a rotating platform in a ³He Ox-

ford Heliox system at temperatures down to 0.235 K in magnetic fields up to 12 T.

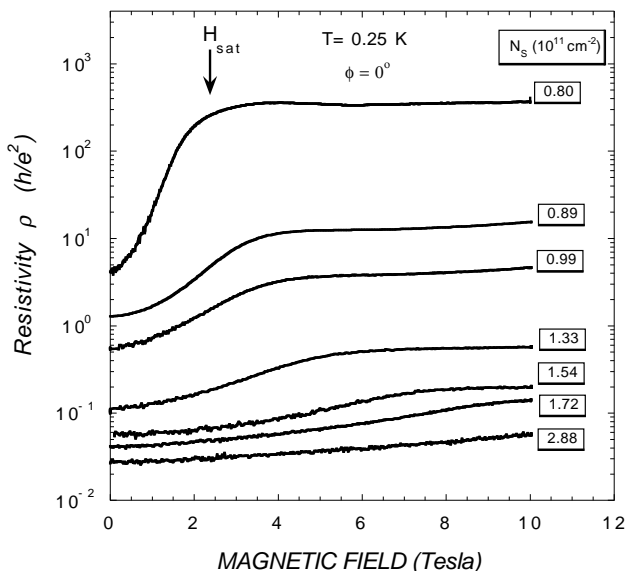


FIG. 1. Resistivity of the 2D electron system in silicon MOSFETs versus in-plane magnetic field for different densities, as labeled. Data are shown at $T = 245$ mK. The arrow indicates H_{sat} for electron density $n_s = 0.80 \times 10^{11} \text{ cm}^{-2}$.

Measurements were first taken with the plane of the sample oriented parallel to the magnetic field [11]. The resistance, R_{xx} , is shown in Fig. 1 as a function of field for different fixed gate voltages spanning densities between $n_s = 0.8 \times 10^{11} \text{ cm}^{-2}$ and $n_s = 2.88 \times 10^{12} \text{ cm}^{-2}$ (the zero field critical density for the metal-insulator transition is $n_c \approx 0.84 \times 10^{11} \text{ cm}^{-2}$). Consistent with earlier findings [7,8,10,12,13], the in-plane ($\phi = 0$) magnetoresistance rises dramatically with increasing field and saturates above a density-dependent field $H_{sat}(n_s)$ [14].

The sample was then rotated to make a small angle ϕ

with respect to the field, so that the in-plane component was almost equal to the total field $H_{\parallel} \approx H$, while the projection in the perpendicular direction, $H_{\perp} \approx \phi H$, remained relatively small even in high fields. R_{xx} and R_{xy} were measured simultaneously as a function of magnetic field for fixed angle ϕ , temperature T , and density n_s .

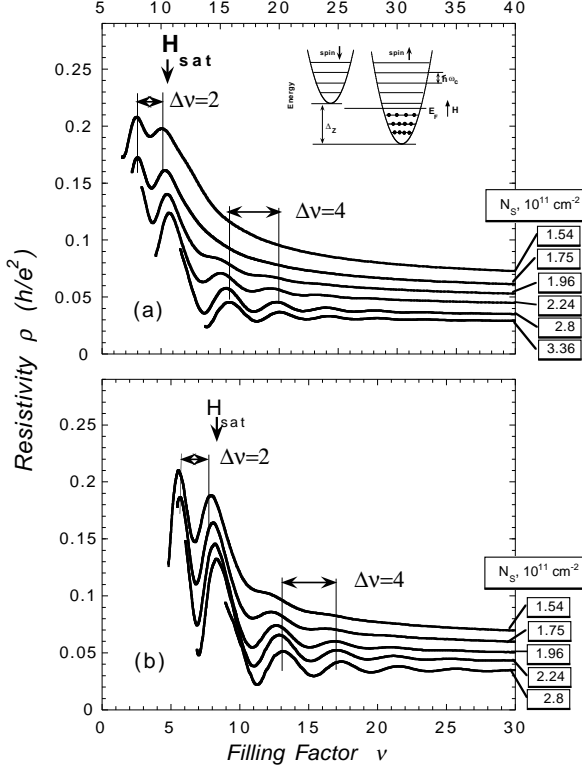


FIG. 2. Resistivity R_{xx} versus electron filling factor $\nu = n_s \Phi_0 / H_{\perp}$ showing SdH oscillations for different electron densities n_s , as labeled. Data are shown at $T = 0.25K$ for two different angles ϕ between the magnetic field and the electron plane: (a) $\phi = 6^\circ$; (b) $\phi = 7.8^\circ$.

For various different densities n_s , Figs. 2 (a) and 2 (b) show the resistance R_{xx} vs filling factor ν at two different angles ϕ between the magnetic field and the 2D plane. Similar curves were obtained at other small angles. The filling factor $\nu = n_s \Phi_0 / H_{\perp}$ was calculated using the relation $n_s = H_{\perp} / (R_{xy} e c)$. The Hall resistivity R_{xy} and Hall coefficient R_H were determined from the low-field data, $R_{xy} = R_H \times H_{\perp}$, (*i. e.* in fields below the onset of quantum oscillations).

For the lowest densities shown in Fig. 2 (a) at angle $\phi = 6^\circ$, the system is in the high-field saturated regime above H_{sat} for filling factor $\nu < 10$. The large arrow indicates H_{sat} for $n_s = 1.54 \times 10^{11} \text{ cm}^{-2}$. Quantum oscillations are clearly evident superimposed on the large plateau value of R_{xx} at small ν . In this region the period of the SdH oscillations corresponds to a change in filling

factor $\Delta\nu_{sat} = 2$ (including the two-fold valley degeneracy for a 2D layer of (100) silicon). For higher filling factors $\nu > 10$ where the 2D electron system is below saturation ($H < H_{sat}$), the period of the SdH oscillations is twice as long, namely $\Delta\nu = 4$. Similar behavior is shown for a bigger angle in Fig. 2 (b), where the larger perpendicular component gives rise to stronger SdH oscillations; here the period doubling is found above $\nu \approx 8$.

The period $\Delta\nu = 2$ of the oscillations at $H > H_{sat}$ corresponds to complete spin polarization of the electrons. There are several scenarios that could account for a transition to full polarization in strong magnetic fields, depending on the nature of the ground state of the system at $H = 0$ [6], an issue that is currently under debate. Here we restrict the discussion to a simple model within a single-particle description. Using this approach we were able to explain the doubling of the frequency of the SdH oscillations at $H > H_{sat}$. However, the detailed behavior of the oscillations in small perpendicular fields is not fully consistent with this model.

As shown schematically in the inset to Fig. 2, the spin-up and spin-down electron bands are split by the Zeeman energy $\Delta_Z = g\mu_B H$, while the spacing between the Landau levels, $\hbar\omega_c = \hbar e H_{\perp} / mc$, is determined by the perpendicular component of the field. We consider the progression as electrons are added to the system: for small densities, $E_F < \Delta_Z$, electrons are added to Landau levels in the spin-up band only, corresponding to a SdH periodicity $\Delta\nu = 2$ (including a factor 2 for the valley degeneracy in silicon); at high densities, $E_F > \Delta_Z$, twice as many electrons are required to fill both spin-up and spin-down Landau levels, yielding the double period, or $\Delta\nu = 4$ [15]. An equivalent argument holds for fixed density as one reduces the magnetic field. Thus, the shorter period $\Delta\nu = 2$ at $H > H_{sat}$ signals the onset of full polarization of the electron system [16]. The relationship between H_{sat} and complete spin polarization was also found by Okamoto *et al* [13] using a different experimental method.

The observed period-doubling is consistent with this simple model only if the spin-up and spin-down levels are degenerate or nearly so, so that $\alpha = \Delta_Z / \hbar\omega_c = i$ with i an integer. The double period should revert to a single period when $\alpha = i + 1/2$, corresponding to a spin-up Landau level between two spin-down Landau levels. The ratio α can be varied experimentally by changing the angle ϕ , or by using the fact that the electron-electron interaction-enhanced g-factor (and thus Δ_Z) decreases with increasing electron density in silicon MOSFETs [13,17]. By taking data over a broad range of densities, we were able to smoothly vary α by more than 1. Close examination of the data shows that the double period in fields below H_{sat} , although stable over a broad range, does break down in a narrow range of densities that is different for different angles ϕ , as expected within this model.

SdH oscillations reflect changes in electron scattering due to periodic oscillations of the density of states at the Fermi level [18]. For the weak perpendicular fields used in our experiments, there is strong scattering and the SdH oscillations are small [19]. Unlike the situation that prevails in high magnetic fields, where the Landau levels are sharp and well-defined, the density of states is best represented in this regime by a harmonic expansion [17]:

$$D_{\downarrow,\uparrow}(E) = D_0(1 + \epsilon \times \cos(2\pi(E \pm \Delta_Z/2)/\hbar\omega_c) + O(\epsilon^2)) \quad (1)$$

Here E , $\Delta_Z = g\mu_B H$, and $\hbar\omega_c$ are the energy, Zeeman energy and cyclotron energy, respectively. The small parameter $\epsilon = 2\exp(-\pi/(\omega_c\tau)) \ll 1$ [17] is proportional to the Dingle factor [19]. Small variations in the resistivity are proportional to small variations in scattering: $\Delta\rho/\rho = \Delta W/W$. Using the Born approximation, $W \sim \int \delta(E - E_F)D(E)dE$, one can show that:

$$\Delta\rho/\rho = \begin{cases} \epsilon \times \cos(\pi\Delta_Z/\hbar\omega_c)\cos(2\pi E_F^0/\hbar\omega_c), & \Delta_Z < 2E_F^0 \\ \epsilon \times \cos(4\pi E_F^0/\hbar\omega_c), & \Delta_Z > 2E_F^0 \end{cases} \quad (2)$$

Here the Fermi energy E_F is measured from the bottom of the band at $H = 0$, E_F^0 is the Fermi energy at $H = 0$, and $D(E)$ is the total density of states: $D(E) = D_{\uparrow}(E) + D_{\downarrow}(E)$. We assumed $T = 0$ and neglected higher harmonic terms of order ϵ^2 in Eq.(1) as well as higher order corrections due to oscillations of the Fermi energy. This demonstrates that the SdH period changes by a factor of 2 when $\Delta_Z > 2E_F^0$, corresponding to full polarization of the electrons.

The term $A = \epsilon\cos(\pi\Delta_Z/\hbar\omega_c)$ of Eq. (2) depends on the ratio $\alpha = \Delta_Z/\hbar\omega_c$, which is fixed for a given angle and electron density and does not vary with magnetic field. It determines the overall amplitude of the oscillations at fields below H_{sat} , when $\Delta_Z < 2E_F^0$. This amplitude has a maximum when $\alpha = \Delta_Z/\hbar\omega_c = i$ is an integer, corresponding to spin up and spin down densities of states oscillating in phase, and vanishes when $\alpha = i + 1/2$ (see Eq.1). Figure 3 shows data over a narrow region near $\alpha = i + 1/2$ where the amplitude of the first harmonic is small, allowing detailed examination of higher harmonic terms (see Eq.(1)).

Based on the usual assumption that the SdH oscillations are determined by the total density of states, $D(E) = D_{\uparrow}(E) + D_{\downarrow}(E)$, one expects and generally observes [20] the progression illustrated schematically in Fig. 4: a minimum which becomes progressively deeper develops at the center of each maximum (see curves (a) and (b)), gradually splitting it into two separate maxima (curve (c)). Thus, the minima of the second harmonic (curve (c)) are at the positions of the maxima of the first harmonic (curve (a) in Fig. 4).

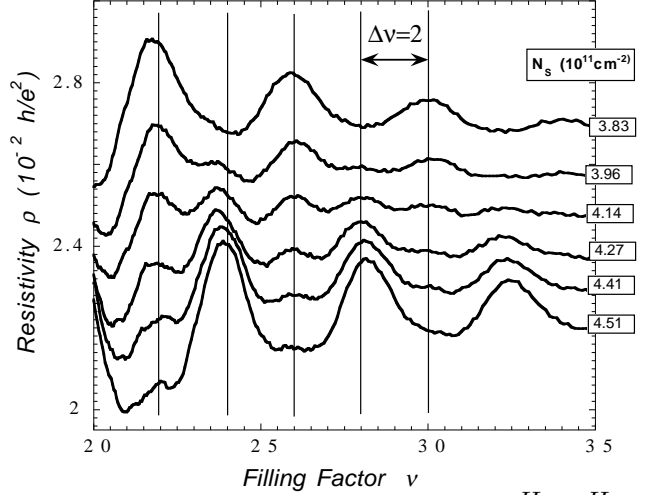


FIG. 2. In magnetic fields below saturation, $H < H_{sat}$, the SdH oscillations are shown for a narrow range of electron densities near $\alpha = \Delta_Z/\hbar\omega_c = g\mu_B H/\hbar\omega_c = (i + 1/2)$; due to the $e - e$ enhancement of the g-factor, each density corresponds to a slightly different value of α . Note that the maxima of the second harmonic ($n_s = 4.14 \times 10^{11} \text{ cm}^{-2}$) are in phase with maxima of the first harmonic ($n_s = 3.83$ and $4.51 \times 10^{11} \text{ cm}^{-2}$).

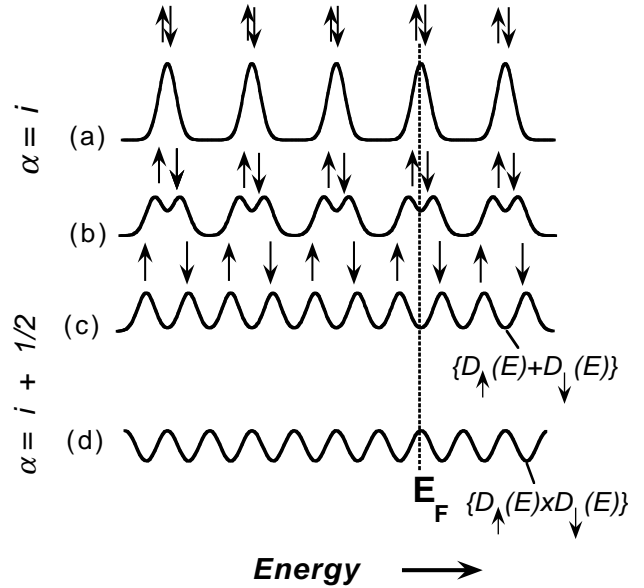


FIG. 3. Schematic of SdH oscillations for a density of states $D(E) = D_{\uparrow}(E) + D_{\downarrow}(E)$ when: (a) the spin-up and spin-down Landau levels are degenerate, $\alpha = \Delta_Z/\hbar\omega_c = i$; (b) $\alpha = i + \delta$ for small δ ; and (c) $\alpha = i + 1/2$. Note that the maxima in (a) and (c) are 180° out of phase. Curve (d) illustrates maxima for the second harmonic in phase with maxima of the first obtained from assuming a scattering probability of the form $W = f(D_{\uparrow}(E) \times D_{\downarrow}(E))$, in agreement with the experimental behavior shown in Fig. 3.

However, careful examination of the data of Fig. 3 shows that the behavior below H_{sat} observed experimentally in silicon MOSFETs is quite different: no minima develop within the maxima, splitting them into two; instead, the maxima simply diminish in amplitude and new neighboring maxima appear and grow in amplitude. The maxima of the first ($n_s = 3.83$ and $4.51 \times 10^{11} \text{ cm}^{-2}$) and second ($n_s = 4.14 \times 10^{11} \text{ cm}^{-2}$) harmonics are in phase (as in curves (a) and (d) of Fig. 4) rather than 180° out of phase. The origin of this unusual behavior is not clear and warrants further careful study. Interestingly, the phase relation between first and second harmonics observed in our experiments can be obtained within the single particle model used earlier if one considers the product of spin-up and spin-down densities of states, $W = f(D_\uparrow(E) \times D_\downarrow(E))$, rather than their sum; curve (d) of Fig. 4 is the result of such a calculation. This suggests there is a sizable contribution to the electron scattering from events that depend on the overlap of spin-up and spin-down densities of states, perhaps reflecting enhanced scattering of electrons of opposite spin.

In summary, measurements of small-angle Shubnikov-de Haas oscillations indicate that the period of the oscillations changes by a factor of two at the magnetic field H_{sat} above which the resistance has reached saturation. We attribute the abrupt change in period to the onset of full polarization of the electron spins. The period doubling in fields below H_{sat} is stable with respect to the angle between the magnetic field and the 2D plane, and is observed for all electron densities except in a narrow interval, where the amplitude of the first harmonic of the SdH oscillations vanishes and the second harmonic is observable. The phase observed for the second harmonic relative to the first is consistent with SdH oscillations due to scattering events that depend on the overlap instead of the sum of the spin-up and spin-down densities of states at the Fermi level. This unusual behavior may reflect the importance of many-body interactions in the 2D system.

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